Exercise 1. Which of the following are sets?
(a) $1,2,3$
(b) $\{1,2\}, 3$
(c) $\{\{1\}, 2\}, 3$
(d) $\{1,\{2\}, 3\}$
(e) $\{1,2, a, b\}$.

Exercise 2. Determine the cardinality of each of the following sets:
(a) $A=\{1,2,3,4,5\}$
(b) $B=\{0,2,4, \ldots, 20\}$
(c) $C=\{25,26,27, \ldots, 75\}$
(d) $D=\{\{1,2\},\{1,2,3,4\}\}$
(e) $E=\{\emptyset\}$
(f) $F=\{2,\{2,3,4\}\}$.

Exercise 3. Write each set in the form $\{x \in \mathbb{Z} \mid p(x)\}$, where $p(x)$ is a property concerning $x$.
(a) $A=\{-1,-2,-3, \ldots\}$
(b) $B=\{-3,-2, \ldots, 3\}$
(c) $C=\{-2,-1,1,2\}$.

Exercise 4. The set $E=\{2 x \mid x \in \mathbb{Z}\}$ can be described by listing its elements, namely $E=\{\ldots,-4,-2,0,2,4 \ldots\}$. List the elements of the following sets in a similar manner.
(a) $A=\{2 x+1 \mid x \in \mathbb{Z}\}$
(b) $B=\{4 n \mid n \in \mathbb{Z}\}$
(c) $C=\{3 q+1 \mid q \in \mathbb{Z}\}$.

Exercise 5. For $A=\{2,3,5,7,8,10,13\}$, let

$$
B=\{x \in A \mid x=y+z, \text { where } y, z \in A\} \text { and } C=\{r \in B \mid r+s \in B \text { for some } s \in B\}
$$

Determine $C$.
Exercise 6. For each of the following give examples of three sets $A, B$ and $C$ such that
(a) $A \subseteq B \subset C$
(b) $A \in B, B \in C$, and $A \notin C$
(c) $A \in B$ and $A \subset C$.

Exercise 7. Which of the following sets are equal?

$$
\begin{gathered}
A=\{n \in \mathbb{Z}| | n \mid<2\}, B=\left\{n \in \mathbb{Z} \mid n^{3}=n\right\}, C=\left\{n \in \mathbb{Z} \mid n^{2} \leq n\right\} \\
D=\left\{n \in \mathbb{Z} \mid n^{2} \leq 1\right\}, E=\{-1,0,1\}
\end{gathered}
$$

Exercise 8. Find $\mathcal{P}(\mathcal{A})$ and $|\mathcal{P}(A)|$ for $A=\{0, \emptyset,\{\emptyset\}\}$.
Exercise 9. Let $U=\{1,3, \ldots, 15\}$ be the universal set, $A=\{1,5,9,13\}$, and $B=\{3,9,15\}$. Determine the following:
(a) $A \cup B$
(b) $A \cap B$
(c) $A \backslash B$
(d) $B \backslash A$
(e) $\bar{A}$
(f) $A \cap \bar{B}$.

Exercise 10. Give examples of three sets $A, B$, and $C$ such that $B \neq C$ but $B \backslash A=C \backslash A$.

