

Show all work clearly and in order. Justify your answers.

(1) Suppose  $X$  is a continuous random variable with density function

$$f(x) = \begin{cases} 0 & x < -1 \\ \frac{x^2}{3} & -1 \leq x \leq A \\ 0 & x > A \end{cases}$$

(a) Find  $A$  which makes this a true probability density function.

(b) Find  $P(X < 1 | X > 0)$ .

(c) Find the probability that the following function of  $X$  (the random variable from part (a)) is increasing:

$$g(X) = X^4$$